Magnetoelectric multiferroics are compounds with magnetic and electric orders that coexist and are coupled via magnetoelectric interactions.\textsuperscript{1-4} Research in this field is motivated by the promise of devices that can sense and create magnetic polarizations using electric fields and vice versa, thereby creating new functionality as well as improving the speed, energy efficiency, and size of existing circuits. A new class of induced multiferroics has become the topic of intense study in the past few years, in which a magnetic order induces an electric polarization.\textsuperscript{5-13} These materials are either low-dimensional or frustrated magnets in which competing interactions give rise to noncollinear order that breaks spatial inversion symmetry (SIS). This SIS-breaking magnetism couples to the lattice most likely via spin-orbit interactions that lower magnetic energy by distorting the lattice and in the process create electric polarization.

Most magnetoelectrics and multiferroics are transition-metal oxides or fluorides where the magnetoelectric interactions are mediated via superexchange through the oxide and fluoride anions. Magnetoelectric interactions can also be expected in other materials such as organometallic solids but have not yet been clearly established.\textsuperscript{14-16} In this paper we present field-induced multiferroic behavior in an organometallic quantum magnet, CuCl$_2$·2[(CH$_3$)$_2$SO] (CDC), where the Cu spins adopt noncollinear magnetic order that creates an electric polarization in the presence of magnetic fields. Unlike many magnetically induced multiferroics, the magnetic spins do not form a spiral in order to break SIS.

CDC crystallizes in an orthorhombic crystal structure with space-group \textit{Pnma} [see Fig. 1(a)].\textsuperscript{17} The Cu spins form zigzag chains in the crystallographic $a$-$c$ plane, along which the Cu spins are antiferromagnetically coupled via a superexchange interaction $J=1.46$ meV mediated by Cl ions.\textsuperscript{18} Perpendicular to the chains, the Cu atoms are separated by dimethyl sulfoxide groups [Fig. 1(b)] and it is this weaker antiferromagnetic (AFM) interaction that sets the energy scale for three-dimensional long-range order with a Néel temperature $T_N=0.9$ K.\textsuperscript{18} Figure 1(c) shows the evolution of the Cu spins with applied magnetic fields along the $c$ axis, and the phase diagram is summarized in Fig. 2. At zero magnetic field $H$, the magnetic order consists of a collinear AFM arrangement (AFM A) with the magnetic moments pointing along the $c$ axis. As a magnetic field is applied along the $c$ axis, the spins undergo a first-order spin-flop transition into
The Hamiltonian $\mathcal{H}$ must be invariant under all symmetry operations of the space group, and thus $P$ must transform as $L_1 \cdot L_2$. $L_1$ belongs to $\Gamma^5$ and $L_2$ belongs to $\Gamma^8$, thus $P$ transforms as $\Gamma^5 \times \Gamma^8$. As can be seen in Table I, $\Gamma^5 \times \Gamma^8$ contains a single broken mirror plane ($m_{ab}$) implying an allowed uniform $P$ along the $b$ axis. Note that $P$ is a uniform vector field with $Q=0$, and thus invariant under translation, so the glide operation $m_{ab}$ reduces to a simple mirror reflection in the $b$ axis. In this work we present measurements of the electric properties of CDC and we show that an electric polarization indeed occurs along the $b$ axis and is closely coupled to the noncollinear AFM B state.

Table I. Partial list of the irreducible representations of the group $G_k$ for CDC with a commensurate magnetic structure with $k=(0,0,0)$. $\bar{I}$ is an inversion about the origin, $2_a$ denotes a screw axis along $\alpha=a,b,c$ ($180^\circ$ rotation followed by a translation), and $m_{a,b}$ is a glide plane containing the axis $\alpha$ and $b$ (mirror reflection in the plane $\alpha,b$ followed by a translation in that plane).

<table>
<thead>
<tr>
<th>$\Gamma$</th>
<th>$1$</th>
<th>$2_b$</th>
<th>$2_a$</th>
<th>$2_c$</th>
<th>$\bar{I}$</th>
<th>$m_{ac}$</th>
<th>$m_{bc}$</th>
<th>$m_{ab}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Gamma^5$</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
</tr>
<tr>
<td>$\Gamma^8$</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>$\Gamma^5 \times \Gamma^8$</td>
<td>1</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>-1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

Single-crystal samples of CDC were grown from solution. For $P(H)$ measurements, the samples were coated on the a-c faces with silver paint and leads were attached, permitting the magnetoelectric current along the $b$ axis to be recorded with a Stanford Research 570 current to voltage converter. Measurements were performed during the up-sweep of magnetic field pulses with applied magnetic fields along the $c$ axis. The samples were cooled by immersion in $^3$He while rapid $10$ T magnetic pulses with $db/dt$ up to $3.8$ kT/s were applied using a short-pulse capacitatively driven magnet at the National High Magnetic Field Laboratory in Los Alamos, NM (a large $db/dt$ increases the signal to noise levels). The dielectric constant was measured capacitatively in the liquid mixing chamber of an Oxford Kelvinox $400$ $^3$He-$^4$He dilution refrigerator. In order to rule out possible magnetostriction affecting the dielectric constant measurements, magnetostriction was measured separately using a titanium dilatometer mounted in vacuum to the cold finger of the same dilution refrigerator. No signatures of the $3.8$ T transition were observed with a sensitivity to magnetostriction effects $10 \times$ greater than that of the dielectric constant measurements.

Figure 2. (Color online) Magnetic field $H$-Temperature $T$ phase diagram of CDC showing regions of collinear and noncollinear antiferromagnetism (AFM A and B), ferroelectricity, and the staggered paramagnetism (phase C) that occurs at high fields for $H$ along [001]. Data are obtained from peaks in the dielectric constant and magnetoelectric current (this work), neutron diffraction, (Ref. 18) and specific heat (Ref. 19).

The $b$ axis at $0.3$ T. As $H$ is increased further, effective local magnetic fields appear on the Cu sites that alternate from one site to the next along the $a$ axis, and whose strength is proportional to the external magnetic field. These effective fields result from spin-orbit couplings, namely, a staggered $g$ tensor and a Dzyaloshinskii-Moriya interaction. The effective magnetic fields are shown as small blue arrows in the final panel of Fig. 1(c). In response to these staggered fields, the spins gradually rotate from the $b$ axis to the $a$ axis and become noncollinear in the process (AFM B). Between $H =$0.3 and $3.8$ T, the magnetic structure is thus described by two order parameters, one due to the AFM superexchange interactions between the Cu spins and the other due to the spin-orbit-induced staggered fields. Finally, the spins align with the staggered fields along the $a$ axis for $H_c > 3.8$ T (phase C). In addition to the behavior described so far, the spins also can’t along the magnetic field direction with increasing field.

We can show that the noncollinear state between $0.3$ and $3.8$ T (AFM B) breaks SIS and thereby allows an electric polarization $P$ to occur along the $b$ axis. At zero field (AFM A) the magnetic order is commensurate with a wave vector $k=(0,0,0)$. Thus the space group of the magnetic ordering matches that of the lattice, which has eight irreducible representations $\Gamma^1$–$\Gamma^8$. In order to compute whether an electric polarization is possible, we can write down a Landau Hamiltonian with trilinear coupling $\mathcal{H}=P \cdot L_1 \cdot L_2$, where $L_1$ is the magnetization along the $b$ axis that is stabilized by long-range order and $L_2=\chi H$ results from the effective staggered local magnetic fields along the $a$ axis.
MAGNETICALLY INDUCED ELECTRIC POLARIZATION IN...

The direction of $P$ can switch depending on the history of the magnetic field pulses, which demonstrates that it is ferroelectric. When two consecutive magnetic field pulses are applied along the same direction in the $c$ axis (e.g., D followed by E or F followed by G in Fig. 3(a)], the resulting electric polarization for E and G is “positive” along the $b$ axis. The direction of positive and negative is arbitrary. On the other hand, when two consecutive pulses are applied in opposite directions along the $c$ axis (A and B, B and C, C and D, and E and F), the resulting electric polarization for B, C, D, and F is switched into the “negative” direction along the $b$ axis. These measurements were repeated for three samples and found to be reproducible. This type of switching behavior, where the direction of $P$ depends both on the direction of the present magnetic field pulse and the previous one, is unique as far as we know among magnetoelectrics. We note that in addition to the sample being intrinsically hysteretic, there must also be a symmetry-breaking electric field along the $b$ axis in order for the behavior described above to occur. This is further supported by the fact that no electric field poling is required to observe $P$. We speculate that this could result from the influence of Schottky voltages where the capacitor plates contact the sample. These do not contribute a background signal to the data since they are magnetic field independent, however, they can subject the crystal to a symmetry-breaking electric field along $b$. The absence of external electric field poling required to observe $P$ has previously been reported in the magnetoelectric compounds LiNiPO$_4$ and LiCoPO$_4$.

The existence of an electric phase transition is confirmed by dielectric constant measurements along the $b$ axis [Fig. 5(a)]. The signature of the phase transition is a peak in the dielectric constant near $H=3.8$ T. The evolution of the peaks in the dielectric constant [Fig. 5(a)] and the magnetoelectric current [Fig. 5(b)] with temperature are plotted in the phase diagram in Fig. 2 along with previous neutron scattering and specific-heat results. The excellent agreement between the region of noncollinear magnetic order (AFM B) and $P$ in Fig. 2 is evidence for the coexistence and intimate coupling between the electric and magnetic properties of CDC.

Our measurements show that at the upper boundary of the $H$-$T$ phase diagram in Fig. 2, magnetic order and electric polarization are suppressed simultaneously in a continuous phase transition as a function of magnetic field. This transition is not driven by temperature fluctuations, as it occurs at very low temperatures where temperature fluctuations are basically absent. Instead, an earlier work showed that the transition is the result of magnetic field-tuned quantum fluctuations that are associated with a quantum critical point at
Quantum critical point. Quantum critical points have been investigated for cases where one order parameter is critical at the critical point, but we are not aware of any previously observed multiorder quantum critical point in solid matter. Our observation of a magnetoelectrical quantum critical point holds the promise of the study of novel physics in solid materials, such as exotic quantum phases in which two or more order parameters are intimately coupled. Taking advantages of the cross-coupling of two order parameters at a simultaneous critical point, it can be imagined that a magnetic critical point can be tuned with electric fields and vice versa. This adds new ways of conducting time-resolved studies of quantum critical phenomena using the next generation light sources, because electric fields can be controlled on a much smaller time scale than magnetic fields.

In summary, we demonstrate that magnetoelectric interactions mediated via large molecules produce magnetically induced ferroelectricity. The ferroelectric polarization can be switched by short magnetic field pulses in an unusual hysteretic fashion. This initial study, while at low temperatures and with relatively small $P$, provides a motivation for future molecule-based designer magnets based on a wider range of organic ligands with which desired magnetoelectric properties can be fine tuned. The organic ligands provide an array of structures that can lead to frustration and inversion-symmetry breaking including triangles and spirals as well as polar bonds that can form significant electric polarizations, coupled to the magnetic subsystem via the soft crystal structure. Finally, the observation of a magnetoelectric quantum phase transition illustrates the scope of novel physics to be studied in organic magnets.

Work at the National High Magnetic Field Laboratory was supported by the U.S. National Science Foundation through Cooperative Grant No. DMR901624, the State of Florida, and the U.S. Department of Energy. Work at Johns Hopkins University was supported by the National Science Foundation through Grant No. DMR-0306940.

---

FIG. 5. (Color online) (a) Percentage change in the dielectric constant $\varepsilon$ and rate of change in magnetic field $dB/dt$. (b) Magnetoelectric current measurements vs applied magnetic field showing quantum critical phenomena using the next generation light sources, because electric fields can be controlled on a much smaller time scale than magnetic fields.

In summary, we demonstrate that magnetoelectric interactions mediated via large molecules produce magnetically induced ferroelectricity. The ferroelectric polarization can be switched by short magnetic field pulses in an unusual hysteretic fashion. This initial study, while at low temperatures and with relatively small $P$, provides a motivation for future molecule-based designer magnets based on a wider range of organic ligands with which desired magnetoelectric properties can be fine tuned. The organic ligands provide an array of structures that can lead to frustration and inversion-symmetry breaking including triangles and spirals as well as polar bonds that can form significant electric polarizations, coupled to the magnetic subsystem via the soft crystal structure. Finally, the observation of a magnetoelectric quantum phase transition illustrates the scope of novel physics to be studied in organic magnets.

Work at the National High Magnetic Field Laboratory was supported by the U.S. National Science Foundation through Cooperative Grant No. DMR901624, the State of Florida, and the U.S. Department of Energy. Work at Johns Hopkins University was supported by the National Science Foundation through Grant No. DMR-0306940.

---

*Present address: Dresden Hoch-feld Labor, Dresden D-01328, Germany.